

$$\vec{F} = k \frac{q_1 q_2}{r^2} \hat{u}_r = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} \hat{u}_r$$

$$\vec{E} = \frac{\vec{F}}{q} \quad \vec{p} = Q\vec{d}$$

$$d\vec{E} = k \frac{dq}{r^2} \hat{u}_r \quad \vec{E} = k \int \frac{dq}{r^2} \hat{u}_r$$

$$E = \frac{\sigma}{\epsilon_0}$$

$$\Phi_E = \oint_A \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0} = \frac{1}{\epsilon_0} \sum q_i$$

$$Q = \sum q_i = \oint_V \rho dV$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0} \quad \vec{E} = \frac{\sigma}{\epsilon_0} \hat{n}$$

$$\vec{E} = -\nabla V \quad \vec{E} \cdot d\vec{r} = -dV$$

$$V(P_1) - V(P_2) = \int_{P_1}^{P_2} \vec{E} \cdot d\vec{r} \quad V(r) = \frac{q}{4\pi\epsilon_0} \frac{1}{r}$$

$$V(P) = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i} \quad V(P) = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r}$$

$$\vec{E} = -\hat{i}E_x - \hat{j}E_y - \hat{k}E_z = -\hat{i}\frac{\partial V}{\partial x} - \hat{j}\frac{\partial V}{\partial y} - \hat{k}\frac{\partial V}{\partial z}$$

$$\vec{M} = q\vec{d} \times \vec{E} = \vec{p} \times \vec{E}$$

$$U = -qdE \cos \theta = -\vec{p} \cdot \vec{E} \quad U = \vec{p} \cdot \nabla V$$

$$\frac{q_1}{r_1} = \frac{q_2}{r_2} \quad \frac{E_1}{E_2} = \frac{\sigma_1}{\sigma_2} = \frac{r_2}{r_1}$$

$$C = \frac{Q}{\Delta V} = \frac{\epsilon_0 A}{d}$$

$$C = C_1 + C_2 + \dots + C_n$$

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}$$

$$U = \frac{1}{2} V_1 q_1 + \frac{1}{2} V_2 q_2 + \dots + \frac{1}{2} V_n q_n$$

$$U = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} \epsilon_0 E^2 A d \quad u_E = \frac{1}{2} \epsilon_0 E^2$$

$$\vec{E} = \frac{1}{\kappa} \vec{E}_{fri} \quad C = \kappa C_0 = \kappa \frac{\epsilon_0 A}{d} \quad \vec{E} = \vec{E}_f + \vec{E}_b$$

$$\vec{P} = \frac{\Delta \vec{p}}{\Delta V} \quad Q_b = PA \cos \theta = \vec{P} \cdot \vec{A}$$

$$\sigma_b = \frac{Q_b}{A} = \vec{P} \cdot \vec{n} \quad \rho_b = -\nabla \cdot \vec{P}$$

$$\vec{D} = \epsilon_0 \vec{E} + \vec{P} \quad \oint_A \vec{D} \cdot d\vec{A} = Q_f$$

$$\nabla \cdot \vec{D} = \rho_f \quad \vec{P} = \epsilon_0 \chi_e \vec{E}$$

$$\vec{D} = \epsilon_0 \vec{E} + \vec{P} = \epsilon_0 \vec{E} + \epsilon_0 \chi_e \vec{E} \\ = \epsilon_0 (1 + \chi_e) \vec{E} = \epsilon_0 \kappa \vec{E} = \epsilon \vec{E}$$

$$I = \frac{dQ}{dt} = nqAv_d \quad J = \frac{I}{A}$$

$$\vec{J} = nq\vec{v}_d \quad V = RI$$

$$\vec{J} = \sigma \vec{E} \quad \rho = \frac{1}{\sigma} \quad R = \rho \frac{l}{A}$$

$$\rho = \rho_0 [1 + \alpha(T - T_0)]$$

$$R = \sum_{i=1}^n R_i \quad \frac{1}{R} = \sum_{i=1}^n \frac{1}{R_i}$$

$$P = \frac{dU}{dt} = \frac{V dQ}{dt} = VI = RI^2$$

$$I = \frac{dq}{dt}$$

$$\vec{F} = q\vec{v} \times \vec{B} \quad R = \frac{mv}{qB}$$

$$\vec{F} = I \vec{l} \times \vec{B} \quad \vec{F} = I \int (d\vec{l} \times \vec{B}) \quad \vec{T} = I \vec{S} \times \vec{B}$$

$$\vec{m} = NI\vec{S} \quad \vec{T} = \vec{m} \times \vec{B} \quad \vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

$$\omega = \frac{v}{R} = \frac{q}{m} B \quad d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{u}_r}{r^2}$$

$$\vec{B} = \int \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{u}_r}{r^2}$$

$$\oint \vec{B} \cdot d\vec{r} = \mu_0 I_{Tot} = \mu_0 \sum I_i = \mu_0 \int_A \vec{J} \cdot d\vec{A}$$

$$\nabla \times \vec{B} = \mu_0 \vec{J}$$

$$\oint_A \vec{B} \cdot d\vec{A} = 0$$

$$\nabla \cdot \vec{B} = 0$$

$$\oint \vec{B} \cdot d\vec{r} = \mu_0 \left(I + \frac{\partial \Phi_D}{\partial t} \right)$$

$$\nabla \times \vec{B} = \mu_0 \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right)$$

$$\mathcal{E} = - \frac{d\Phi_B}{dt}$$

$$\Phi_B = \int_A \vec{B} \cdot d\vec{A}$$

$$\mathcal{E} = -N \frac{d\Phi_B}{dt}$$

$$\mathcal{E} = \oint \vec{E} \cdot d\vec{l}$$

$$\oint \vec{E} \cdot d\vec{r} = \int_A (\nabla \times \vec{E}) \cdot d\vec{A} = - \frac{d\Phi_B}{dt} = - \frac{d}{dt} \int_A \vec{B} \cdot d\vec{A}$$

$$\nabla \times \vec{E} = - \frac{d\vec{B}}{dt}$$

$$\Phi_B = LI$$

$$\mathcal{E}_L = - \frac{d\Phi_B}{dt} = -L \frac{dI}{dt}$$

$$\tau = \frac{L}{R}$$

$$U = \int_0^I LI' dI' = \frac{1}{2} LI^2$$

$$u_B = \frac{B^2}{2\mu_0}$$

$$u = \frac{1}{2} \epsilon E^2 + \frac{1}{2\mu} B^2$$

$$\mathcal{E}_{21} = -N_2 \frac{d\Phi_{21}}{dt} = -M_{21} \frac{dI_1}{dt}$$

$$M_{21} = M_{12} = M$$

$$\vec{B} = \vec{B}_0 + \mu_0 \vec{M}$$

$$\vec{B}_0 = \mu_0 \vec{H}$$

$$\vec{B} = \mu_0 (\vec{H} + \vec{M})$$

$$\vec{M} = \chi_m \vec{H}$$

$$\mu = \mu_0 (1 + \chi_m)$$

$$\oint \vec{H} \cdot d\vec{r} = \int \vec{J}_{fri} \cdot d\vec{A}$$

$$\vec{m}_L = \frac{-e}{2m_e} \vec{L} = g_L \vec{L}$$

$$m_L = \left(\frac{e}{2m_e} \hbar \right) l = m_B l$$

$$\vec{m}_S = g_S \vec{S} = - \frac{e}{m_e} \vec{S}$$

$$\frac{V_2}{V_1} = \frac{N_2}{N_1}$$

$$I_1 V_1 = I_2 V_2$$

$$\Delta U = \frac{e\hbar}{m_p} B$$

$$L \frac{dI}{dt} + \frac{q}{C} = 0$$

$$q = Q_m \cos(\omega_0 t + \phi)$$

$$\omega_0^2 = \frac{1}{LC}$$

$$U_C = \frac{q^2}{2C}$$

$$U_L = \frac{LI^2}{2}$$

$$U_L + U_C = \frac{Q_0^2}{2C}$$

$$L \frac{dI}{dt} + IR + \frac{q}{C} = 0$$

$$q = Q_m e^{-\frac{t}{\tau}} \cos(\omega t + \phi)$$

$$\tau = \frac{2L}{R}$$

$$\omega = \sqrt{\frac{1}{LC} - \left(\frac{R}{2L} \right)^2} = \sqrt{\omega_0^2 - \frac{1}{\tau^2}}$$

$$X_C = \frac{1}{\omega C}$$

$$X_L = \omega L$$

$$Z = \frac{V_m}{I_m} = \sqrt{R^2 + (X_L - X_C)^2}$$

$$\tan \phi = \frac{X_L - X_C}{R}$$

$$I = I_m \sin(\omega t - \phi)$$

$$\bar{P} = \frac{1}{2} I_m^2 R = I_{rms}^2 R$$

$$\bar{P} = V_{rms} I_{rms} \cos \phi$$

$$\hat{Z} = X + iY = Ze^{i\phi} = Z(\cos \phi + i \sin \phi)$$

$$Z = \sqrt{X^2 + Y^2}$$

$$V = V_m \sin(\omega t) \quad \text{eller} \quad V = V_m \cos(\omega t)$$

$$\hat{V} = V_m e^{i\omega t}$$

$$L \frac{d\hat{I}}{dt} + R\hat{I} + \frac{\hat{Q}}{C} = V_m \cos(\omega t) + iV_m \sin(\omega t)$$

$$\hat{I} = \frac{d\hat{Q}}{dt}$$

$$L \frac{d^2 \hat{I}}{dt^2} + R \frac{d\hat{I}}{dt} + \frac{\hat{I}}{C} = (i\omega) V_m e^{i\omega t}$$

$$\hat{I} = \hat{I}_m e^{i\omega t}$$

$$\hat{I}_m = \frac{V_m}{\left[R + i \left(\omega L - \frac{1}{\omega C} \right) \right]} = \frac{V_m}{R + i(X_L - X_C)}$$

$$\hat{Z} = R + iX = Ze^{i\phi}$$

$$Z = \sqrt{R^2 + X^2}$$

$$\tan \phi = \frac{X}{R} = \frac{X_L - X_C}{R}$$

$$\hat{I}_m = \frac{V_m}{\hat{Z}} = \frac{V_m}{Ze^{i\phi}} = \frac{V_m}{Z} e^{-i\phi}$$

$$I = \text{Im}(\hat{I}) = I_m \sin(\omega t + \phi)$$

$$\text{eller } I = \text{Re}(\hat{I}) = I_m \cos(\omega t + \phi)$$

$$I_m = \frac{V_m}{Z} = \frac{V_m}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$\hat{Z}_R = R$$

$$\hat{Z}_L = i\omega L$$

$$\hat{Z}_C = \frac{1}{i\omega C} = -\frac{i}{\omega C}$$

$$\hat{Z} = \hat{Z}_1 + \hat{Z}_2$$

$$\frac{1}{\hat{Z}} = \frac{1}{\hat{Z}_1} + \frac{1}{\hat{Z}_2}$$

$$\hat{V} = \hat{Z}\hat{I}$$

Maxwells ligninger m.m.:

$$\oint \vec{E} \cdot d\vec{r} = -\frac{d}{dt} \int_A \vec{B} \cdot d\vec{A} \quad \nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\oint_A \vec{D} \cdot d\vec{A} = \int_V \rho dV \quad \nabla \cdot \vec{D} = \rho$$

$$\oint \vec{H} \cdot d\vec{r} = \int_A \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right) \cdot d\vec{A}$$

$$\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\int_A \vec{B} \cdot \hat{n} dA = 0 \quad \nabla \cdot \vec{B} = 0$$

$$\vec{D} = \epsilon \vec{E} = \kappa \epsilon_0 \vec{E}$$

$$\vec{B} = \mu \vec{H} = \kappa_M \mu_0 \vec{H}$$

$$E_{2t} = E_{1t}$$

$$D_{1n} = D_{2n}$$

$$\nabla^2 \vec{E} = \epsilon_0 \mu_0 \frac{\partial^2 \vec{E}}{\partial t^2}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

$$\nabla^2 \vec{B} = \epsilon_0 \mu_0 \frac{\partial^2 \vec{B}}{\partial t^2}$$

$$\vec{E} = \vec{E}_0 \sin(kz - \omega t)$$

$$B_0 = \frac{kE_0}{\omega} = \frac{E_0}{c}$$

$$v = \frac{1}{\sqrt{\kappa \epsilon_0 \mu_0}} = \frac{c}{\sqrt{\kappa}} = \frac{c}{n}$$

$$u = u_E + u_B = 2u_E = \epsilon_0 E^2$$

$$I = \frac{\delta E}{A \delta t} = \frac{c \delta E}{A \delta x} = \frac{c \delta E}{\delta V} = cu$$

$$I = \frac{1}{\mu_0} EB$$

$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$$

$$p = \frac{S}{c}$$

$$p = \frac{2S}{c}$$

$$I = I_0 \cos^2 \theta$$

$$\vec{E} = \hat{i} E_x \cos(kz - \omega t) + \hat{j} E_y \cos(kz - \omega t + \phi)$$

$$E_1 + E_r = E_2$$

$$S_1 = S_r + S_2$$

$$S = \frac{1}{\mu_0} EB = \frac{n}{\mu_0 c} E^2$$

$$\frac{S_r}{S_1} = \left(\frac{n_1 - n_2}{n_1 + n_2} \right)^2$$

$$\frac{S_2}{S_1} = \frac{4n_1^2}{(n_1 + n_2)^2}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{1}{s} + \frac{1}{s'} \approx \frac{2}{R}$$

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f}$$

$$\frac{n_1}{s} + \frac{n_2}{s'} \approx \frac{n_2 - n_1}{R}$$

$$\frac{n_1}{f} = (n_2 - n_1) \left(\frac{1}{R_a} - \frac{1}{R_b} \right)$$

$$m = -\frac{s'}{s}$$

$$M = \frac{25}{f(\text{cm})}$$

$$\phi = 2\pi \frac{l}{\lambda} = 2\pi \frac{d \sin \theta}{\lambda}$$

$$\phi = \pm m(2\pi) \text{ eller } d \sin \theta_m = \pm m\lambda$$

$$d \sin \theta_{m'} = \pm \left(m' + \frac{1}{2} \right) \lambda$$

$$E_T = \left[2E_0 \cos\left(\frac{\phi}{2}\right) \right] \sin\left(\omega t + \frac{\phi}{2}\right)$$

$$I_T = 4I_0 \cos^2\left(\frac{\phi}{2}\right) = 4I_0 \cos^2\left(\frac{\pi d \sin \theta}{\lambda}\right)$$

$$I_T = 4I_0 \cos^2\left[\left(\frac{\pi d}{\lambda L}\right)x\right]$$

$$E_T = E_0 \sum_{n=0}^{N-1} \sin(\omega t + n\phi)$$

$$E_T = \left[\frac{\sin(N\phi/2)}{\sin(\phi/2)} \right] E_0 \sin\left\{ \omega t + (N-1)\frac{\phi}{2} \right\}$$

$$I_T = I_0 \left[\frac{\sin(N\phi/2)}{\sin(\phi/2)} \right]^2$$

$$\Delta\phi_{1/2} = 2\pi / N$$

$$d \sin \theta_m = \pm m\lambda \quad m = 0, 1, 2, \dots$$

$$\Delta\theta_{1/2} = \frac{1}{N \sqrt{(d/\lambda)^2 - m^2}}$$

$$D = \frac{m}{d \cos \theta_m}$$

$$\Delta\lambda > \frac{\lambda}{Nm}$$

$$\beta = \frac{\pi a \sin \theta}{\lambda}$$

$$I = I_0 N^2 \frac{\sin^2 \beta}{\beta^2}$$

$$I = I_M \frac{\sin^2 \beta}{\beta^2}$$

$$I_T = 4I_M \frac{\sin^2 \beta}{\beta^2} \cos^2\left[\left(\frac{\pi d}{\lambda L}\right)x\right]$$

$$\Delta\theta > \frac{\lambda}{D}$$

$$x \propto \frac{1}{\omega_0^2 - \omega^2} \cos(\omega t)$$

$$\frac{1}{n^2} = 1 - \frac{K}{\omega_0^2 - \omega^2}$$